

# Package ‘robumeta’

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**Type** Package

**Title** Robust Variance Meta-Regression

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**Suggests** clubSandwich, R.rsp

**Description** Functions for conducting robust variance estimation (RVE) meta-regression using both large and small sample RVE estimators under various weighting schemes. These methods are distribution free and provide valid point estimates, standard errors and hypothesis tests even when the degree and structure of dependence between effect sizes is unknown. Also included are functions for conducting sensitivity analyses under correlated effects weighting and producing RVE-based forest plots.

**URL** <https://github.com/zackfisher/robumeta>

**BugReports** <https://github.com/zackfisher/robumeta/issues>

**License** GPL-2

**LazyData** true

**RoxygenNote** 7.2.2

**VignetteBuilder** R.rsp

**NeedsCompilation** no

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corrdat	<i>Data for Fitting Correlated Effects Model</i>
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### Description

Fictional data used in TannerTanner-Smith and Tipton (2013).

### Format

A dataframe containing 172 effect sizes from 39 studies used in Tanner- Smith and Tipton (2013).

### Source

<https://my.vanderbilt.edu/emilytannersmith/training-materials/>

### References

Tanner-Smith E.E., Tipton, E. (2013) Robust variance estimation with dependent effect sizes: practical considerations including a software tutorial in Stata and SPSS. *Research Synthesis Methods*. ISSN 1759-2887.

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corrdat.sm	<i>Data for Fitting Correlated Effects Model With Small-Sample Corrections</i>
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### Description

Data used in Tipton (2013).

### Format

A dataframe containing 300 effect sizes from 28 studies used in Tipton (2013).

**Source**

Elizabeth Tipton

**References**

Tipton, E. (in press) Small sample adjustments for robust variance estimation with meta-regression. *Psychological Methods*.

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forest.robust

*Forest Plots for Robust Variance Estimation Meta-Analysis*

---

**Description**

forest.robust In meta-analysis, forest plots provide a graphical depiction of effect size estimates and their corresponding confidence intervals. The forest.robust() function in **robustmeta** can be used to produce forest plots for RVE meta-analyses. The function requires the **grid** package and is based on examples provided in (Murrell, 2011). As is the case with traditional forest plots, point estimates of individual effect sizes are plotted as boxes with areas proportional to the weight assigned to that effect size. Importantly, here the weight is not necessarily proportional to the effect size variance or confidence intervals, since the combined study weight is divided evenly across the study effect sizes. Two-sided 95% confidence intervals are calculated for each effect size using a standard normal distribution and plotted along with each block. The overall effect is included at the bottom of the plot as a diamond with width equivalent to the confidence interval for the estimated effect. The RVE forest function is designed to provide users with forest plots which display each individual effect size used in the meta-analysis, while taking into account the study- or cluster-level properties inherent to the RVE analysis. As such, the user must specify columns from their original dataset that contain labels for the study or cluster and for the individual effect sizes.

**Usage**

```
forest.robust(x, es.lab, study.lab, ...)
```

**Arguments**

x	An intercept-only RVE model previously fit using the robust() function..
es.lab	A vector of labels to be used to individual effect sizes in the forest plot. Labels for individual effect sizes might be “Math Score” or “Reading Score” for a meta-analysis that included such measures or as simple as “Effect Size 1” and “Effect Size 2.”
study.lab	A vector of labels to be used to identify study (or cluster) level groupings in the forest plot. For instance, labels for the study column might be author names with corresponding publication years.
...	Additional arguments to be passed to the forest function. Any number of additional columns can be specified to be plotted along side the confidence interval column and can be specified with the following syntax ``arg1'' = ``arg2'' where ``arg1'' is the title of the column on the forest plot, and ``arg2'' is the name of the column from the original data.frame that contains the information to be displayed alongside the estimates and confidence intervals.

## References

- Hedges, L.V., Tipton, E., Johnson, M.C. (2010) Robust variance estimation in meta-regression with dependent effect size estimates. *Research Synthesis Methods*. **1**(1): 39–65. Erratum in **1**(2): 164–165. DOI: 10.1002/jrsm.5
- Murrell P (2011). R Graphics. CRC/Taylor & Francis. ISBN 9781439831762.
- Tipton, E. (in press) Small sample adjustments for robust variance estimation with meta-regression. *Psychological Methods*.

## Examples

```
# Load data
data(oswald2013.ex1)

# Run intercept only model.
oswald_intercept <- robu(formula = effect.size ~ 1, data = oswald2013.ex1,
                        studynum = Study, var.eff.size = var.eff.size,
                        rho = 0.8, small = TRUE)

# Create forest plot.
forest.robu(oswald_intercept, es.lab = "Crit.Cat", study.lab = "Study",
            "Effect Size" = effect.size, # optional column
            "Weight" = r.weights)      # optional column
```

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group.center

*Convenience function for calculating group-centered covariates.*

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## Description

Creates a within-study (or within-cluster) version of the covariate in question.

## Usage

```
group.center(var, grp)
```

## Arguments

var	The covariate to be group centered.
grp	A vector corresponding to the group identification.

## Value

A column or vector containing the group.centered covariate.

## Examples

```
# Load data
data(corrdat)

# Create a group centered covariate
males_c <- group.center(corrdat$males, corrdat$studyid)
```

---

group.mean	<i>Convenience function for calculating group-mean covariates.</i>
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## Description

Creates a between-study (or between-cluster) version of the covariate in question.

## Usage

```
group.mean(var, grp)
```

## Arguments

var	The covariate containing the values to be group averaged.
grp	The group from which the average should be calculated.

## Value

A column or vector containing the group.mean covariate.

## Examples

```
# Load data
data(corrdat)

# Create a group mean covariate
age_m <- group.mean(corrdat$age, corrdat$studynum)
```

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 hedgesdat

*hedgesdat*


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**Description**

Data from a meta-analysis on the effectiveness of phonics reading instruction by Ehri, Nunes, Stahl and Willows (2001). Data reported in Hedges, Tipton, and Johnson (2010) with example.

**Format**

A dataframe containing 179 effect sizes from 66 different studies

**Source**

Hedges, Tipton, and Johnson (2010)

**References**

Ehri, L.C., Nunes, S.R., Stahl, S.A., Willows, D.M. (2001) Systematic phonics instruction helps children learn to read: Evidence from the National Reading Panel's meta-analysis. *Review of Educational Research*. **71**, 393–447.

Hedges, L.V., Tipton, E., Johnson, M.C. (2010) Robust variance estimation in meta-regression with dependent effect size estimates. *Research Synthesis Methods*. **1**(1): 39–65. Erratum in **1**(2): 164–165. DOI: 10.1002/jrsm.5

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 hierdat

*Data for Fitting Hierarchical Effects Model*


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**Description**

Fictional data used in TannerTanner-Smith and Tipton (2013).

**Format**

A dataframe containing 68 effect sizes from 15 studies used in Tanner- Smith and Tipton (2013).

**Source**

<https://my.vanderbilt.edu/emilytannersmith/training-materials/>

**References**

Tanner-Smith E.E., Tipton, E. (2013) Robust variance estimation with dependent effect sizes: practical considerations including a software tutorial in Stata and SPSS. *Research Synthesis Methods*. ISSN 1759-2887.

oswald2013

*IAT Criterion-Related Correlations***Description**

Data from a meta-analysis on IAT conducted by Oswald et al., (2013) examining the predictive validity of the Implicit Association Test (IAT) and various explicit measures of bias for a variety of criterion measures of discrimination. Included in the dataset are the study level correlations between IAT scores and some criterion measure of discrimination.

**Format**

A dataframe containing 308 effect sizes from 46 studies.

[,1]	Study	Factor
[,2]	Crit.Domain	Factor
[,3]	IAT.ID	Integer
[,4]	IAT.Focus	Factor
[,5]	Crit.ID	Integer
[,6]	Crit.Cat	Factor
[,7]	Scoring	Factor
[,8]	Target	Factor
[,9]	Type	Factor
[,10]	Sample.ID	Integer
[,11]	N	Integer
[,12]	R	Numeric

**Source**

Oswald FL, Mitchell G, Blanton H, Jaccard J, Tetlock PE (2013) Predicting ethnic and racial discrimination: a meta-analysis of IAT criterion studies. *Journal of Personality and Social Psychology*, 105(2), 171-192. ISSN 1939-1315. doi:10.1037/a0032734. PMID: 23773046.

**References**

Oswald FL, Mitchell G, Blanton H, Jaccard J, Tetlock PE (2013) Predicting ethnic and racial discrimination: a meta-analysis of IAT criterion studies. *Journal of Personality and Social Psychology*, 105(2), 171-192. ISSN 1939-1315. doi:10.1037/a0032734. PMID: 23773046.

oswald2013.ex1

*IAT Criterion-Related Correlations***Description**

Data from a meta-analysis on IAT conducted by Oswald et al., (2013) examining the predictive validity of the Implicit Association Test (IAT) and various explicit measures of bias for a variety of criterion measures of discrimination. Included in the dataset are the study-level correlations between IAT scores and criterion measures of neurological activity or response latency from the original oswald2013 dataset.

**Format**

A dataframe containing 32 effect sizes from 9 studies.

[,1]	Study	Factor
[,2]	Crit.Domain	Factor
[,3]	IAT.ID	Integer
[,4]	IAT.Focus	Factor
[,5]	Crit.ID	Integer
[,6]	Crit.Cat	Factor
[,7]	Scoring	Factor
[,8]	Target	Factor
[,9]	Type	Factor
[,10]	Sample.ID	Integer
[,11]	N	Integer
[,12]	R	Numeric
[,13]	effect.size	Numeric
[,14]	var.eff.size	Numeric

**Source**

Oswald FL, Mitchell G, Blanton H, Jaccard J, Tetlock PE (2013) Predicting ethnic and racial discrimination: a meta-analysis of IAT criterion studies. *Journal of Personality and Social Psychology*, 105(2), 171-192. ISSN 1939-1315. doi:10.1037/a0032734. PMID: 23773046.

**References**

Oswald FL, Mitchell G, Blanton H, Jaccard J, Tetlock PE (2013) Predicting ethnic and racial discrimination: a meta-analysis of IAT criterion studies. *Journal of Personality and Social Psychology*, 105(2), 171-192. ISSN 1939-1315. doi:10.1037/a0032734. PMID: 23773046.



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predict.robust	<i>Prediction method for a robumeta object.</i>
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### Description

predict.robust produces the predicted mean and confidence interval of a fitted robumeta model object given a prediction vector.

### Usage

```
## S3 method for class 'robust'
predict(object, pred.vector, level = 0.95, ...)
```

### Arguments

object	A fitted robumeta model object.
pred.vector	A prediction vector containing the new covariate values.
level	Confidence level.
...	Additional arguments to predict.

### Details

- **intercept** If an intercept is included in the robumeta model, the first element should always be 1, representing the intercept, followed by the covariate values in appropriate order. If the robumeta model does not have an intercept, the prediction vector should begin with the first covariate value.
- **variable** For continuous variables, use the variable value as the corresponding element value in pred.vector. For a categorical variable the original variable value should be transformed to match the coding system used in the robumeta model (e.g. dummy coding, deviation coding, etc.).
- **NA** If the vector contains NAs, predict.robust will remove the corresponding covariates from the original data, and refit a new robumeta model. The prediction and confidence interval will be estimated based on the new model.

```
robust_mod <- robust(LOR1 ~ study_design + duration + service_hrs,
                    data = dropoutPrevention,
                    studynum = studyID,
                    var.eff.size = varLOR,
                    modelweights = "HIER",
                    small = TRUE)
```

In this robumeta model, the first covariate is a categorical variable that contains three levels: "Matched" (33 percent, dummy code: 00), "Randomized"(24 percent, 01) and "non-match non-randomized"(43 percent, 10). The corresponding prediction vector begins with 1 (intercept), and followed by 0, 0, the dummy code for "Matched". The last two elements are 38 and 5, the values for duration and service\_hrs.

```
predict(object = robu_mod, pred.vector = c(1,0,0,38,5),level = 0.95)
```

If we do not know the value of duration, the prediction vector should be `c(1,0,0,NA,5)`. `predict.robust()` will refit a new model without the covariate duration, and the prediction will be based on it.

```
predict(object = robu_mod, pred.vector = c(1,0,0,NA,5),level = 0.95)
```

### Value

prediction the predicted value based on the prediction vector.

se The standard error for the predicted mean.

t The t-statistic calculated based on the predicted mean.

df The small sample corrected degrees of freedom of the distribution of the t-statistic.

lower The lower bound of the confidence interval for the predicted mean.

upper The upper bound of the confidence interval for the predicted mean.

---

```
print.robust
```

*Outputs Model Information*

---

### Description

Prints relevant information from `robu` function.

### Usage

```
## S3 method for class 'robust'
print(x, digits = 3, ...)
```

### Arguments

<code>x</code>	Object from <code>robust</code> class.
<code>digits</code>	Controls the number of digits to print when printing numeric values.
<code>...</code>	Additional arguments to be passed to the fitting function.

### References

Hedges, L.V., Tipton, E., Johnson, M.C. (2010) Robust variance estimation in meta-regression with dependent effect size estimates. *Research Synthesis Methods*. **1**(1): 39–65. Erratum in **1**(2): 164–165. DOI: 10.1002/jrsm.5

Tipton, E. (in press) Small sample adjustments for robust variance estimation with meta-regression. *Psychological Methods*.

## Examples

```
# Load data
data(hierdat)

### Small-Sample Corrections - Hierarchical Dependence Model
HierMod <- robu(formula = effectsize ~ binge + followup + sreport
                + age, data = hierdat, studynum = studyid,
                var.eff.size = var, modelweights = "HIER", small = FALSE)

print(HierMod) # Output results
```

---

 robu

*Fitting Robust Variance Meta-Regression Models*


---

## Description

robu is used to meta-regression models using robust variance estimation (RVE) methods. robu can be used to estimate correlated and hierarchical effects models using the original (Hedges, Tipton and Johnson, 2010) and small-sample corrected (Tipton, 2013) RVE methods. In addition, robu contains options for fitting these models using user-specified weighting schemes (see the Appendix of Tipton (2013) for a discussion of non-efficient weights in RVE).

## Usage

```
robu(
  formula,
  data,
  studynum,
  var.eff.size,
  userweights,
  modelweights = c("CORR", "HIER"),
  rho = 0.8,
  small = TRUE,
  ...
)
```

## Arguments

formula	An object of class "formula". A typical meta-regression formula will look similar to $y \sim x_1 + x_2 \dots$ , where $y$ is a vector of effect sizes and $x_1 + x_2 \dots$ are (optional) user-specified covariates. An intercept only model can be specified with $y \sim 1$ and the intercept can be omitted as follows $y \sim -1 + \dots$ .
data	A data frame, list or environment or an object coercible by <code>as.data.frame</code> to a data frame.

<code>studynum</code>	A vector of study numbers to be used in model fitting. <code>studynum</code> must be a numeric or factor variable that uniquely identifies each study.
<code>var.eff.size</code>	A vector of user-calculated effect-size variances.
<code>userweights</code>	A vector of user-specified weights if non-efficient weights are of interest. Users interested in non-efficient weights should see the Appendix of Tipton (2013) for a discussion of the role of non-efficient weights in RVE).
<code>modelweights</code>	User-specified model weighting scheme. The two available options are <code>modelweights = "CORR"</code> and <code>modelweights = "HIER"</code> . The default is <code>"CORR"</code> . See Hedges, Tipton and Johnson (2010) and Tipton (2013) for extended explanations of each weighting scheme.
<code>rho</code>	User-specified within-study effect-size correlation used to fit correlated ( <code>modelweights = "CORR"</code> ) effects meta-regression models. The value of <code>rho</code> must be between 0 and 1. The default value for <code>rho</code> is 0.8. <code>rho</code> is not specified for hierarchical ( <code>modelweights = "HIER"</code> ) effects models.
<code>small</code>	<code>small = TRUE</code> is used to fit the meta-regression models with the small-sample corrections for both the residuals and degrees of freedom, as detailed in Tipton (2013). Users wishing to use the original RVE estimator must specify <code>small = FALSE</code> as the corrected estimator is the default option.
<code>...</code>	Additional arguments to be passed to the fitting function.

### Value

<code>output</code>	A data frame containing some combination of the robust coefficient names and values, standard errors, t-test value, confidence intervals, degrees of freedom and statistical significance.
<code>n</code>	The number of studies in the sample <code>n</code>
<code>.</code>	
<code>k</code>	The number of effect sizes in the sample <code>k</code>
<code>.</code>	
<code>k descriptives</code>	the minimum <code>min.k</code> , mean <code>mean.k</code> , median <code>median.k</code> , and maximum <code>max.k</code> number of effect sizes per study.
<code>tau.sq.</code>	<code>tau.sq</code> is the between study variance component in the correlated effects meta-regression model and the between-cluster variance component in the hierarchical effects model. <code>tau.sq</code> is calculated using the method-of-moments estimator provided in Hedges, Tipton, and Johnson (2010). For the correlated effects model the method-of-moments estimator depends on the user-specified value of <code>rho</code> .
<code>omega.sq.</code>	<code>omega.sq</code> is the between-studies-within-cluster variance component for the hierarchical effects meta-regression model. <code>omega.sq</code> is calculated using the method-of-moments estimator provided in Hedges, Tipton, and Johnson (2010) erratum.
<code>I.2</code>	<code>I.2</code> is a test statistics used to quantify the amount of variability in effect size estimates due to effect size heterogeneity as opposed to random variation.

## References

Hedges, L.V., Tipton, E., Johnson, M.C. (2010) Robust variance estimation in meta-regression with dependent effect size estimates. *Research Synthesis Methods*. **1**(1): 39–65. Erratum in **1**(2): 164–165. DOI: 10.1002/jrsm.5

Tipton, E. (in press) Small sample adjustments for robust variance estimation with meta-regression. *Psychological Methods*.

## Examples

```
# Load data
data(hierdat)

# Small-Sample Corrections - Hierarchical Dependence Model
HierModSm <- robu(formula = effectsize ~ binge + followup + sreport
                  + age, data = hierdat, studynum = studyid,
                  var.eff.size = var, modelweights = "HIER", small = TRUE)

print(HierModSm) # Output results
```

---

sensitivity

*Sensitivity Analysis for Correlated Effects RVE*

---

## Description

sensitivity is used to assess the impact of differing rho values on the correlated effects meta-regression model.

## Usage

```
sensitivity(x)
```

## Arguments

x                    A dataframe containing values of rho, tau squared, coefficient estimates, and standard errors.

## References

Hedges, L.V., Tipton, E., Johnson, M.C. (2010) Robust variance estimation in meta-regression with dependent effect size estimates. *Research Synthesis Methods*. **1**(1): 39–65. Erratum in **1**(2): 164–165. DOI: 10.1002/jrsm.5

Tipton, E. (in press) Small sample adjustments for robust variance estimation with meta-regression. *Psychological Methods*.

**Examples**

```
# Correlated Effects Model
CorrMod <- robu(formula = effectsize ~ followup + males + binge + college,
                data = corrdat, studynum = studyid, var.eff.size = var,
                rho = .8, modelweights = "CORR", small = FALSE)

sensitivity(CorrMod) # Output sensitivity
```

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